

The n th term of a geometric sequence is U_n , where $U_n = 48\left(\frac{1}{4}\right)^n$

a) Find U_1

b) Find the sum to infinity of the series

$$a) U_n = 48 \left(\frac{1}{4}\right)^n$$

For U_n , $n=1$

$$U_1 = 48 \left(\frac{1}{4}\right)^1$$

$$U_1 = 48 \times \frac{1}{4}$$

$$U_1 = 48 \div 4$$

$$U_1 = 12$$

b)

$$U_1 = 12$$

$$r = \frac{1}{4}$$

Series is convergent because $-1 < r < 1$

$$S_\infty = \frac{U_1}{1-r}$$

$$S_\infty = \frac{12}{1-\frac{1}{4}}$$

$$S_\infty = \frac{12}{\frac{3}{4}}$$

$$S_\infty = 12 \div \frac{3}{4}$$

$$S_\infty = 12 \times \frac{4}{3}$$

$$S_\infty = 12 \times \frac{1}{3} \times 4$$

$$S_\infty = 4 \times 4$$

$$S_\infty = 16$$